

# Options

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CS522 – Spring 2005

## Calls

- A European **call** (on stock) confers the right, but not the obligation, to **acquire** one share of the underlying stock at a fixed, predetermined price (the strike price).
- Notation:
  - $t$  = time when the contract is entered into;
  - $T$  = time when the right can be exercised (maturity or expiration date);
  - $K$  = strike price (in \$/share)
  - $c(t, T; K)$ , sometimes simplified to  $c(T; K)$ ,  $c(T)$ , or  $c(K)$ , when the other arguments are implied.

## Calls (2)

- An American call is like a European call, except that the option can be exercised **anytime** from inception to expiration. Notation  $C(t, T; K)$ ,  $C(T; K)$ ,  $C(T)$ ,  $C(K)$ .
- The holder of an option contract is the individual who can exercise the associated rights; s/he is **long** in the option. The individual who sold the right is **short** in the option. This is true for puts as well.

## Puts

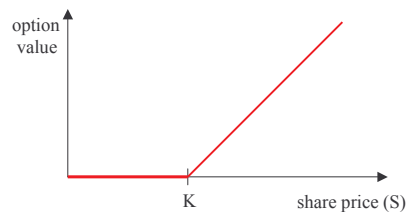
- A European **put** (on stock) confers the right, but not the obligation, to **sell** one share of the underlying stock at a fixed, predetermined price (the strike price).
- Notation:  
t = time when the contract is entered into;  
T = time when the right can be exercised (maturity or expiration date);  
K = strike price (in \$/share)  
 $p(t, T; K)$ , sometimes simplified to  $p(T; K)$ ,  $p(T)$ , or  $p(K)$ , when the other arguments are implied.

## Puts (2)

- An American **put** is like a European call, except that the option can exercised **anytime** from inception to expiration.  
Notation  $P(t, T; K)$ ,  $P(T;K)$ ,  $P(T)$ ,  $P(K)$ .

## Payoff Diagrams at Expiration

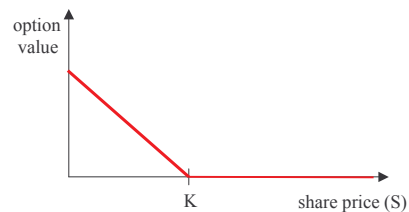
•Calls with strike K



The upside is potentially infinite. The payoff is always non-negative.

$$C(T)=c(T)=\max(0, S(T)-K)$$

•Puts with strike K



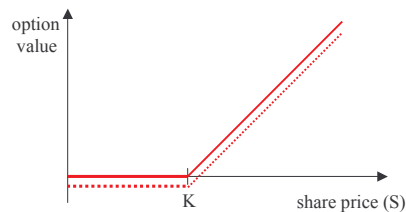
The upside is limited at K. The payoff is always non-negative.

$$P(T)=p(T)=\max(K-S(T), 0)$$

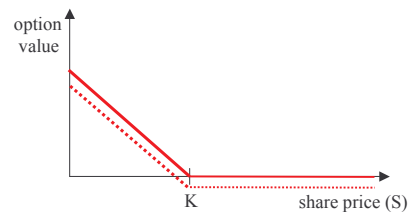
Note: we ignore transaction costs!

## Transaction Costs

•Calls with strike K



•Puts with strike K



Transaction costs decrease the payoff by a constant amount.  
One should still exercise the option if the share price is over K.

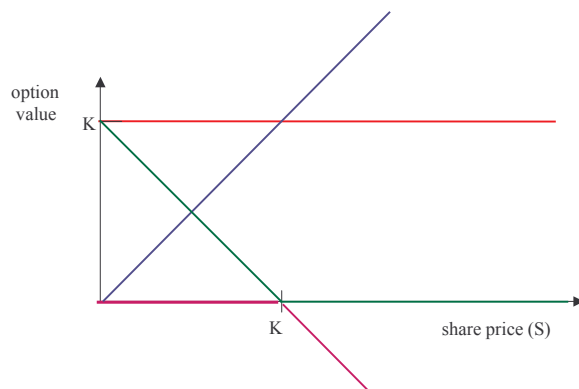
## Market Players

- Several categories of players; they need each other to achieve their goals.
- **Hedgers:** want to protect their investment against adverse movements in the markets, and they are willing to pay for it, typically obtaining lower, but safer returns.
- **Speculators:** are willing to assume risk in order to achieve higher, but more variable returns. Sometimes they lose a lot.

## Using Calls and Puts

- Market players can build portfolios of shares, calls, and puts that achieve their goals.
- We will continue to ignore transaction costs.
- As calls and puts expire, the portfolios lose their initial properties.

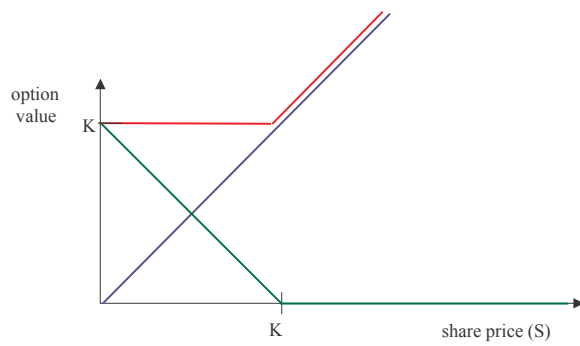
## Indifference to Price Changes



$$S(T) + P(T, T; K) - C(T, T; K)$$

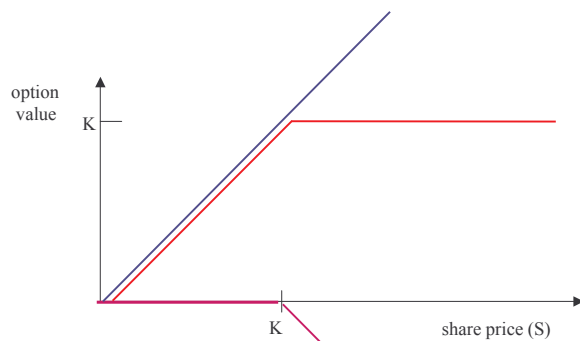
Note: At  $T$ ,  $P(T, T; K) = p(T, T; K)$  and  $C(T, T; K) = c(T, T; K)$ .

## Insure Against Downside



$$S(T) + P(T, T; K)$$

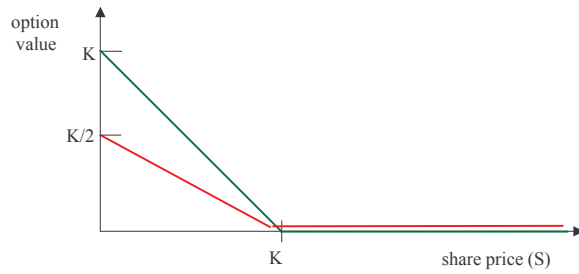
## Give Up the Upside



$$S(T) - C(T, T; K)$$

What can induce a rational person to give up the upside potential?

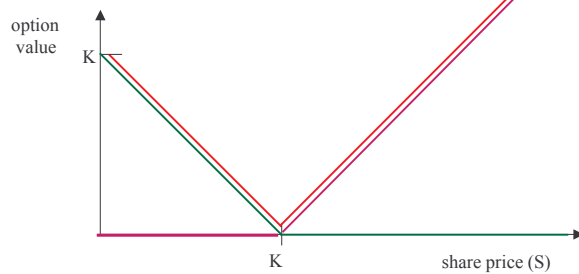
## Not All Slopes Are Equal to $\pm 1$ !



$$\frac{1}{2}P(T, T; K)$$

Does it make sense to even consider such situations?

## Straddle



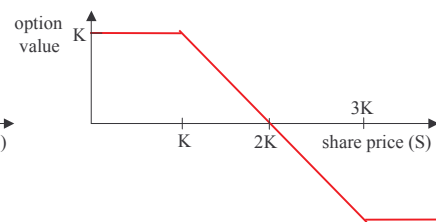
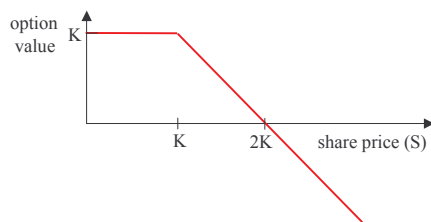
$$P(T, T; K) + C(T, T; K)$$

The profit increases as the stock price moves away from  $K$ .

## Payoffs & Traders' Market View

- Let us say that we have a definite view of the market. Say, we are pessimistic.
- If we know what will happen, we can always make money.  
Note 1: "Knowing" is really, really hard.  
We could say "hope" instead.  
Note 2: We need further assumptions.
- We want to make money if share prices go down.

## The Pessimist's View



- |  |  |
|--|--|
| 1. Makes money if prices are under $K$ . | 1. Makes money if prices are under $K$ . |
| 2. Payoff increases as $S$ decreases.    | 2. Payoff increases as $S$ decreases.    |
| 3. Losses are <b>unlimited</b> .         | 3. Losses are limited.                   |

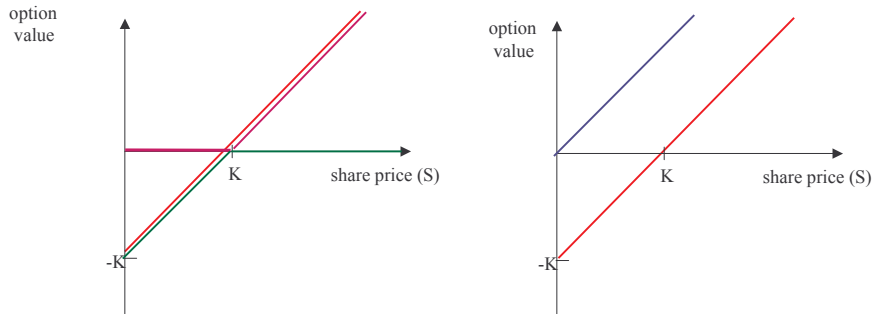
Which contract would a risk-averse investor prefer?

Which payoff will be cheaper?

Write down the portfolios corresponding to these payoffs!



## Put-Call Parity at T



$$C(T,T;K) - P(T,T;K) = S(T) - K$$

## Reading Market Data

The cost of buying a call or a put is typically much less than the price of the underlying asset. This makes it easy to achieve **leveraged** positions. Can be dangerous!

| Rank | Stock | Option            | Option Symbol | Close | Change            | Volume | Volume Change     | Open Interest | Open Interest Change |
|------|-------|-------------------|---------------|-------|-------------------|--------|-------------------|---------------|----------------------|
| 1    | INTC  | MAR05<br>22.5 Put | NQOXX         | 0.175 | -0.05<br>(-22.2%) | 41489  | 27633<br>(199.4%) | 39393         | 7183<br>(22.3%)      |

After Hours (RT-ECN): 23.98  $\uparrow$  0.01 (0.04%)

|                |                         |               |               |
|----------------|-------------------------|---------------|---------------|
| Last Trade:    | 23.99                   | Day's Range:  | 23.86 - 24.49 |
| Trade Time:    | Feb 28                  | 52wk Range:   | 19.64 - 30.14 |
| Change:        | $\uparrow$ 0.10 (0.42%) | Volume:       | 78,984,655    |
| Prev Close:    | 24.09                   | Avg Vol (3m): | 70,840,318    |
| Open:          | 24.15                   | Market Cap:   | 149.39B       |
| Bid:           | 22.10 $\times$ 200      | P/E (ttm):    | 20.70         |
| Ask:           | 24.25 $\times$ 1000     | EPS (ttm):    | 1.16          |
| 1y Target Est: | 27.68                   | Div & Yield:  | 0.32 (1.33%)  |

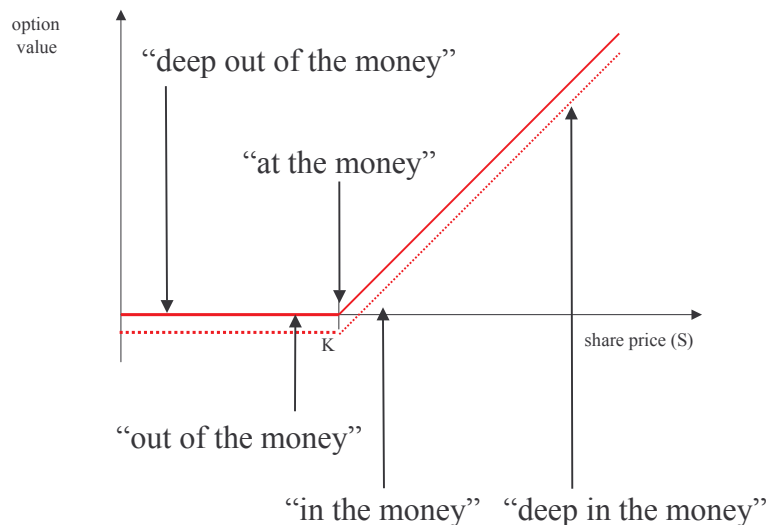
## Options Markets

- This time we will not provide many details.
- Options are derivatives, their value depends on the value of another underlying instrument.
- Historically, people have been mostly interested in options on commodities.
- Options are traded OTC and on exchanges (since April 1973, on the CBOE).
- Options trading on exchanges are standardized. Why?

## Options Markets (2)

- Only a relatively small set of delivery dates and strike prices are available at any time.
- Option contracts are written in multiples of 100 shares of the underlying stock.
- Delivery is usually not requested; payoffs are settled in cash.
- If one wishes to get out of an option contract, this can be done at any time by closing out the position (i.e. selling a  $c(t,T;K)$  if one is long in the same call).

## In/Out of the Money



## What's an Option's True Worth?

- We know the payoff at the expiration.
- We would like to know the value at inception and at any intermediate time  $t'$  between  $t$  and  $T$ . The market price should equal the value of the option.
- Let us denote an arbitrary option by  $O$ . We must have that  $O(t, T; K)$  at time  $t'$  has the same value as  $O(t', T; K)$ . Why?  
Options have no "memory," i.e. the past (time  $< t$ ) does not influence their value at time  $= t$ .
- We will thus only consider the value of  $O(t, T; K)$  at time  $t$ .